Buyer Resistance for Cartel versus Merger*

Vikram Kumar,† Robert C. Marshall,‡ Leslie M. Marx,§ and Lily Samkharadze¶

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Abstract

Procurement practices are affected by uncertainty regarding suppliers’ costs, the nature of competition among suppliers, and uncertainty regarding possible collusion among suppliers. Buyers dissatisfied with bids of incumbent suppliers can cancel their procurements and resolicit bids after qualifying additional suppliers. Recent cartel cases show that cartels devote considerable attention to avoiding such resistance from buyers. We show that in a procurement setting with the potential for buyer resistance, the payoff to firms from forming a cartel exceeds that from merging, and does so by a magnitude that can offset efficiency gains from a merger. Thus, firms considering a merger may have an incentive to collude instead. We discuss implications for antitrust and merger policy.

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†vuk119@psu.edu, Department of Economics, Penn State University
‡rcm10@psu.edu, Department of Economics, Penn State University
.§marx@duke.edu, Fuqua School of Business, Duke University
¶likasamkharadze@gmail.com, Department of Economics, University of Mannheim
1 Introduction

In the late 1800s, although neither mergers nor cartels were illegal, many firms chose to form a cartel rather than merge. Although cartels in this period did not need to hide their existence to avoid prosecution, they operated in a clandestine manner to disguise their presence from their customers. This suggests that a key benefit of cartel formation versus merger is that a cartel can take advantage of customer beliefs that the policing action of competition is still in place.

Procurements commonly include an element of “buyer resistance,” whereby buyers that are concerned that the policing action of competition is not adequate can resist high prices. As shown through a review of municipal procurements (see Appendix C), which are typically organized as sealed-bid competitive procurements, buyer resistance to high prices often comes in the form of buyers rejecting all bids in an initial procurement and then after some delay holding a new procurement with additional bidders present. Colluding firms often face buyer resistance that limits their ability to implement collusive price increases.

Considering the tradeoffs between merger and cartel formation, a merged entity does not incur costs associated with disguising its existence from its customers, and a merged entity does not have to overcome the difficulties faced by cartels associated with incentives for cartel members to secretly deviate from the terms of a collusive agreement (see Stigler, 1946).

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1Merger as an effort to monopolize were not recognized as a violation of the law until the resolution of Northern Securities v. U.S. (197 U.S. 400) (hereafter Northern Securities) in 1904. The operation of a cartel was not recognized as a violation until decisions of 1897 and thereafter (Bittlingmayer, 1985, p.77).

2As described by George Bittlingmayer (1985, p.77): “Perhaps as much as one-half of U.S. manufacturing capacity took part in mergers during the years 1898 to 1902. These mergers frequently included most of the firms in an industry and often involved firms that had been fixing prices or that had been operated jointly through the legal mechanism of an industrial trust. ... The Sherman Antitrust Act was passed in 1890, and the first crucial decisions making price fixing illegal – Trans-Missouri (1897), Joint Traffic (1898), and Addyston (1899) – occurred just before or during the first stages of the merger wave. Merger of competing firms remained unchallenged until 1904.”


4The ability of federal procurement officials to reject all bids is formalized in the U.S. Federal Acquisition Regulations, which state: “Invitations may be cancelled and all bids rejected before award but after opening when ... (6) All otherwise acceptable bids received are at unreasonable prices, or only one bid is received and the contracting officer cannot determine the reasonableness of the bid price; (7) The bids were not independently arrived at in open competition, were collusive, or were submitted in bad faith.” (U.S. Federal Acquisition Regulations, Section 14.404 Rejection of bids, https://www.acquisition.gov/Far/reissue/FARvol1ForPaperOnly.pdf)

5In the Vitamins Cartel, which included firms BASF, Roche, and Daiichi, “When BASF’s customers resisted the increase, Roche supported the rise by also announcing an increase.... According to Daiichi, the concerted increase was unsuccessful because of customer resistance....” (EC Decision in Vitamins, par. 325) In the Cartonboard Cartel, where colluding firms sold product to packaging manufacturers referred to as converters, “The converters have on some occasions resisted a proposed price increase for cartonboard on the ground that their own customers would in their turn refuse to accept a price increase for packaging ....” (EC Decision in Cartonboard, par. 19)
1964). Thus, in the absence of agency problems and transaction costs inherent in large firms as in Williamson (1985) or Coase (1937), one might expect a merged entity to be able to duplicate any actions that a cartel can undertake and also potentially take additional actions that a cartel cannot. However, a clandestine cartel may be able to take advantage of customer beliefs that the policing action of competition might still be in place, and thus may face reduced buyer resistance.

In this paper, we examine whether one can understand the decision by firms to form a cartel rather than merge as an equilibrium response to buyer resistance. We consider a model in which firms have an opportunity to merge, collude, or remain noncooperative and in which there is a procurement process with the possibility for buyer resistance, which we model as the ability of the buyer to reject initial bids and hold a new procurement after inviting additional bidders to participate.6

As we show, firms may find a cartel structure to be more profitable than a merger when customers are uncertain as to whether nonmerged firms are operating as a cartel or not. We show that in an environment where buyers are strategic, firms prefer to collude rather than merge.

We are able to quantify the expected payoff gain from collusion versus a merger within the context of our model. We show that the incremental payoff from collusion relative to a merger with no cost efficiencies can be substantial and that the efficiency effects of a merger may not be sufficient to offset these gains. Evidence from prosecuted cartels is consistent with a choice of collusion over merger. For 42% of cartel cases reported by the European Commission between 2001 and 2010, in the period after the end of the illegal conduct, some subset of cartel firms were involved in mergers, acquisitions, or joint ventures. Clearly, merger efficiencies were inadequate during the cartel period to induce these firms to choose merger over cartel, although such a choice was apparently feasible.

While cartels and horizontal mergers have been widely studied in the past,7 there is not much work that addresses these two forms of industrial organization as potential alternatives for incumbent firms.8 An exception is Bittlingmayer (1985), which directly addresses why many firms preferred colluding over merging in the past. Building on Sharkey (1973),

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6In Section 2, we discuss the details of one such episode that received attention in the landmark Addyston Pipe conspiracy. For additional examples, see Appendix C.2.

7On cartels, see the survey article by Levenstein and Suslow (2006) and the references therein. On mergers, see the survey article by Mookherjee (2006) and the references therein.

8One could offer a Coasian (1937) explanation for the choice between a cartel and a merged entity. The trade-off between the costs of maintaining and operating a cartel versus the cost of running a large merged entity due to, say, diseconomies of scale or agency problems, is likely to influence the “merge or cartelize” decision for firms. See Nocke and White (2007) for the effects of vertical mergers on incentives to collude and Kovacic et al. (2009) for effects of horizontal mergers. For an examination of the tradeoff between merger and predation, see, e.g., Persson (2004).
Bittlingmayer (1985) emphasizes the role of fixed costs in industries with a small number of firms and uncertain demand. Bittlingmayer argues that a cartel may be a cheaper form of organization than a merger in cyclical industries, where costs can be recovered during periods of high demand and cooperation between firms is required only occasionally when demand is low.9

In a durable goods environment, Ausubel and Deneckere (1987) show that a cartel has the commitment power to maintain static monopoly prices while a monopolist lacks this ability. Thus, industry profits are higher when incumbent firms collude rather than merge.10

Ganslandt, Persson, and Vasconcelos (2012) consider whether merger choices can be affected by the sustainability of collusion post merger, showing that mergers that create moderate asymmetries may facilitate collusion when there is an indivisible cost of collusion.

The remainder of this paper is organized as follows. Section 2 provides motivating background and empirical evidence. Section 3 presents our model. Section 4 provides our results. Section 5 considers merger efficiencies. Section 6 concludes.

2 Background

The U.S. v. Addyston Pipe and Steel Co.11 case of 1898 is considered to be a landmark event in antitrust history (Bittlingmayer, 1982). In 1894, six southern manufacturers of cast iron pipes,12 which are used to transport water and gas by cities and municipalities, entered into a conspiracy.13 Before a procurement, the cartel members would participate in a pre-
auction knock-out, bidding on the per-ton bonus payment they would make into the cartel pool. The winner — the firm that bid the highest per-ton bonus payment — would represent the cartel in the actual procurement and bid an amount fixed by the “representative board” of the cartel.\textsuperscript{14} The other cartel members would “protect” this bid by submitting phantom bids.\textsuperscript{15}

After about two years of operation, suspicion about the existence of the cartel was raised when at a procurement in Atlanta, cartel members that were within a hundred miles of the city bid one to two dollars higher than a noncartel company (R.D. Wood & Co.) that was a thousand miles away. All bids were rejected as being too high and a new procurement was held. Anniston (for whom Atlanta was reserved) then bid considerably lower than its original bid, suggesting that bids were not competitive in the first instance.\textsuperscript{16}

An initial civil suit against the defendants in 1896 was decided in favor of the cartel, but in a landmark 1898 verdict, Howard Taft declared the cartel illegal.\textsuperscript{17} The \textit{Addyston} case, along with the railroad cartel cases involving the Trans-Missouri Freight Association and the Joint Traffic Association,\textsuperscript{18} was instrumental in defining illegal collusion under Section 1 of the Sherman Act (Bittlingmayer, 1985).

Cartels were not illegal under the common law that existed before the Sherman Act,\textsuperscript{19} although agreements among cartel members may have been deemed unenforceable if their primary function was restraint of trade (Jones, 1921, p.17; Hylton, 2003, pp.30—37). The Sherman Act of 1890 made cartel agreements criminal offenses and thus a matter for public enforcement authorities.\textsuperscript{20}

While the \textit{Addyston}, \textit{Trans-Missouri}, and \textit{Joint Traffic} verdicts set precedents for \textit{collusion} being a criminal offense under the Sherman Act, in 1904 the \textit{Northern Securities} verdict set a precedent for \textit{merging} to form a monopoly being an offense under the Act.\textsuperscript{21} In fact in 1895, in \textit{U.S. v. E.C. Knight}, the Supreme Court decided in favor of the American Sugar

\begin{flushleft}
\textit{Addyston Pipe and Steel et al. vs The United States} (hereafter \textit{Addyston} Transcript of Record), p.296.
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\textsuperscript{14} \textit{Addyston} Transcript of Record, p.70.
\textsuperscript{15} \textit{Addyston} Transcript of Record, p.296.
\textsuperscript{16} \textit{Addyston} Transcript of Record, p.299.
\textsuperscript{17} The Supreme Court upheld the decision in 1899 in the first unanimous decision in a Sherman Act case (Whitney, 1958).
\textsuperscript{19} According to Hylton (2003, p.37), “no common law action for conspiracy to restrain trade existed.” Thorelli (1954, p.53) argues that “the vast majority of cases at common law were private suits between parties to restrictive arrangements.” For a more detailed discussion see Torelli (1954, pp.36–53).
\textsuperscript{20}See Hylton (2003, pp. 90-104) for a detailed discussion of the Sherman Act and the common law principles.
\textsuperscript{21} \textit{Northern Securities v. U.S.}, 197 U.S. 400, was an historic Supreme Court case under the Sherman Act involving the merger of major railroad companies, which lead to the creation of Northern Securities. In 1904, the merged entity was dissolved.
Refining Company, which was a virtual monopoly formed through the consolidation of sugar refineries.\textsuperscript{22} Thus, there was a period between 1895 and 1904 when a large consolidation was not deemed illegal by the Supreme Court, but a cartel was.

In a little more than a year after the antitrust decision against the Addyston cartel by the Sixth Circuit in 1898, the cartel members merged in 1899 to form the United States Cast Iron Pipe and Foundry Company (USCIP&F).\textsuperscript{23} The firms initially chose collusion over merging, and only upon being prosecuted for collusion did they decide to merge. In fact, prior to the first wave of industrial mergers, which happened between 1898 and 1904, the chosen form of cooperation among firms in a wide range of industries seems to have been collusion rather than merger (Jones, 1921, p.6).

A review of the ten largest (in net value) manufacturing industry groups according to the U.S. census of 1900, shows that at least eight of those ten industry groups include industries in which firms that had previously cartelized went on to merge. (See Appendix C.) For example, in the meat packing industry, cartel members agreed to merge just ten days after their cartel was disrupted by a Department of Justice investigation.\textsuperscript{24}

For more recent evidence, we review the European Commission decisions in cartel cases available on the European Commission website. (See Appendix C.) We focus on the 55 industrial cartel decisions between 2001 and 2010 for which there is a published decision. For these cases, we find evidence of mergers, acquisitions, or joint ventures among at least two of the co-conspirators after the end of the cartel period in 23 (42\%) of the cases. Thus, it seems that when authorities take away collusion as an option, firms sometimes turn to mergers, acquisitions, or joint ventures as second-best options.\textsuperscript{25}

For the 25 EC decisions for industrial cartels issued in years 2001–2005, we classify the demand side of the market (i.e., parties purchasing from the cartel) as relatively concentrated or relatively fragmented, with the expectation that significant buyer resistance is more likely to come from relatively concentrated buyers. Among the cases where significant buyer resistance was less likely, 40\% have mergers, acquisitions, or joint ventures among at least two of

\textsuperscript{22} U.S. v. E.C. Knight, 156 U.S. 1 (hereafter E.C. Knight).

\textsuperscript{23} Whitney (1958, vol. 2, p.7). The event involved the merger of more than two firms and so might also be referred to as a consolidation.

\textsuperscript{24} Whitney (1958, vol. 1, p.33). As an example from the “chemicals and allied products” industry group, there was a cartel in gunpowder manufacturing called the Gunpowder Trade Association from 1872 to 1902 (by which time 95\% of the industry was in the association). In 1902, Du Pont Co. took over the second-largest manufacturer, Lafflin & Rand, which was also part of the association. This and subsequent mergers were consistent with the advice of Du Pont’s lawyers, who cited Addyston as an example of collusion being perceived as illegal and cited E.C. Knight, where consolidation resulting in a virtual monopoly was allowed, as an example of a merger being less likely to be prosecuted (Bittlingmayer, 1985).

\textsuperscript{25} It is also possible for a merger to trigger the detection of a cartel. For example, cartel conduct is may be detected during the due diligence process by the purchaser or evidence of collusion may be identified during the merger investigation. One must be cautious about inferring causality.
the co-conspirators after the end of the cartel period, but only 20% among the cases where significant buyer resistance was more likely. This evidence is consistent with the results of this paper showing that the payoff to merging (or other observable coordination) is reduced in environments with buyer resistance.

3 Model

3.1 Overview

We begin by considering a benchmark model that does not account for merger efficiencies, and then we introduce merger efficiencies.

We consider a procurement setting with a buyer, two incumbent sellers, and one potential new seller. In terms of the number of players, this is minimal if we are going to allow for buyer resistance by a strategic buyer that enhances competition by inviting a previously unqualified seller to participate.

We consider two coordination regimes, one in which sellers must compete noncooperatively and another in which sellers may form a cartel or merge. If the sellers merge, this is observed by all players. If the sellers do not merge, then the sellers observe whether a cartel has been formed, but the buyer does not and so is uncertain about the existence of a cartel. The cost environment for the sellers is either low cost or high cost. The cost environment determines the distribution from which sellers’ individual costs are drawn. The cost environment is observed by the sellers but not by the buyer. Sellers’ individual costs are their own private information. The buyer purchases through a competitive procurement, but the buyer retains the right to suspend the procurement and invite the potential new seller as a bidder. It is costly to the buyer to do this, but it may allow the buyer to obtain a better price.

After observing the initial bids, the buyer forms beliefs about the cost state and whether there is collusion. There is a cost to the buyer of reprocurement, so if the cost state were known to be high, then there would be nothing to be gained from reprocurement and the buyer would be better off accepting high initial bids. But if the cost state is low, then the buyer may prefer to reject high initial bids because of the potential for obtaining a lower price through reprocurement. Firms would like to submit high bids but are disciplined by the threat that the buyer might reject the bids and qualify additional sellers in response.

We show that in this model, the two incumbent sellers are able to obtain higher profits if

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26 For other approaches to modeling buyer resistance, see Harrington and Chen (2006) and Marshall, Marx, and Raiff (2008).
they form a cartel than if they merge. Relative to the case of merged firms, when nonmerged firms submit high bids, the buyer, who is uncertain about the existence of the cartel, attaches a greater probability to high bids being the result of high costs. Thus, given that the new seller only reduces the buyer’s expected payment in a low-cost environment, the buyer is less likely to incur the cost to invite the new seller when a cartel (whose existence is not observable to the buyer) submits a high bid compared to when a merged entity submits a high bid. As a result, in the absence of merger efficiencies, firms find it more profitable to collude than to merge.

3.2 Framework

There is one buyer that wishes to procure a single item by means of a first-price procurement. We assume the buyer has value greater than 1 for the item. There are three potential sellers: two incumbent sellers, which we label seller 1 and seller 2, and one new potential seller, which we label seller 3. We assume that with probability \( \rho \in (0, 1) \), the cost state is low and each seller \( i \) draws its cost \( x_i \) independently from the uniform distribution on zero to one, and that with probability \( 1 - \rho \), the cost state is high and all sellers’ costs are equal to 1. All sellers and the buyer know the distributional source of costs conditional on the low or high-cost state. Sellers observe whether they are in the low-cost or high-cost state, but the buyer does not. The buyer knows that costs are bounded above by one and so does not accept bids greater than 1.

We assume that with probability \( \xi \in (0, 1) \), sellers 1 and 2 are able to form a cartel or merge if they so choose. However, with probability \( 1 - \xi \), communication costs or other organizational impediments (or, in the case of collusion, aversion to illegal activity) prevent sellers 1 and 2 from being able to form a cartel or merge. The sellers observe whether the environment permits them to form a cartel or merge, but the buyer does not, although if the sellers choose to merge, that is observed by the buyer. We model both a merged entity and a cartel as a bidder that draws two costs and then bids to maximize its payoff based on the minimum of those two costs.

We assume that the buyer can qualify seller 3 to participate as a bidder and reconduct the procurement at cost \( k \) to the buyer.\(^{27}\)

The timing and information in the model is as follows:

**Stage 0 (industry structure):** The cooperation state determining the ability of the

\(^{27}\)In many industries potential suppliers have to be pre-qualified before they are allowed to participate in the procurement. Supplier qualification process is usually costly for the procurer as it typically involves verification of quality and reliability requirements, on-site visits, and verification of insurance coverages and credit-worthiness.
sellers to form a cartel or merge is realized and observed by the sellers but not by the buyer: cartel or merger is possible with probability $\xi$ and not possible with probability $1 - \xi$. If the formation of a cartel or merger is possible, then sellers 1 and 2 choose between merging and forming a cartel.\footnote{We can also allow the firms to have the option of choosing to remain as noncooperative bidders, but in equilibrium this option is not chosen.} A decision to merge is observed by all players. A decision by sellers 1 and 2 to form a cartel is observed by the sellers, including seller 3, but not by the buyer. The state of the sellers’ costs is realized and observed by the sellers but not by the buyer: low with probability $\rho$ and high with probability $1 - \rho$.

**Stage 1 (initial bidding):** The buyer announces a procurement and all players observe the buyer’s reprocurement cost $k$. Sellers 1 and 2 draw independent costs $x_1$ and $x_2$ from the cost distribution, which is determined by the cost state.\footnote{If the cost state is realized prior to the sellers’ choice of industry organization, then the sellers are indifferent between merging, colluding, and remaining independent in the high-cost state. If we suppose some small cost to the sellers to merge or collude, then firms in the high-cost state would prefer to remain independent. In that case, upon observing nonmerged firms, the buyer would believe it is either facing a cartel in the low-cost state or noncooperative firms. The buyer’s posterior belief on the low-cost state following a bid of 1 would be the same as described above, so the equilibrium of the continuation game would be unchanged.} A merged entity or cartel bids based on its cost being $\min\{x_1, x_2\}$. In the noncooperation state, sellers bid noncooperatively.

**Stage 2 (evaluation of bids):** After observing the bids, the buyer decides either to make an award to the low bidder at the amount of its Stage-1 bid or to void the initial bids and incur cost $k$ to reconduct the procurement with seller 3 as an additional qualified bidder, in which case Stage 3 is reached.

**Stage 3 (reprocurement):** Sellers draw new costs from either the low-cost or high-cost distribution according to cost state and submit bids.\footnote{In our model, we assume that bidders draw costs for Stage 1 and then draw new costs for Stage 3 if that stage is reached. One could also assume that sellers 1 and 2 only draw costs once and that those costs carry over to Stage 3 if that stage is reached. In such a model, it seems clear that merged and colluding sellers would still have an incentive to bid 1 in the low-cost state in some cases, with a cartel doing so for a greater range of cost draws than a merged firm, so our main result would continue to hold. However, in the low-cost state, the bidding strategies in Stage 3 and in Stage 1 for bids less than 1 would be more complicated. Seller 3 would make inferences from Stage-1 bids as to the costs of its rivals in the Stage-3 procurement and would bid more aggressively if the inference was that its rivals had lower costs. Given this, bidders in Stage-1 would have an incentive to adjust their bids to affect seller 3’s inference. The buyer’s incentive to reject Stage-1 bids would depend on how the Stage-3 bidding would unfold should the buyer qualify seller 3 and reconduct the procurement. In constructing the model as we did, it was our assessment that our results were better illuminated by sidestepping this additional complexity.} The buyer makes an award to the low bidder at the amount of its Stage-3 bid.

We use Perfect Bayesian Equilibrium (PBE) as our solution concept.\footnote{If the sellers always choose to collude in the favorable cooperation state, then following the observation of a merged entity, the buyer’s beliefs as to the cost state are not pinned down by Bayes’ Rule. However, in} In analyzing the equilibria of this game, it will be useful to break it into two separate games. We define the
“merger game” to be the game above but with $\xi = 1$ and where the sellers’ are required to merge. We define the “cartel game” to be the game above, but where sellers are required to act as a cartel when the cooperation state allows them to do so. This allows us to analyze the tradeoff to sellers between merging and forming a cartel and so identify equilibria of the larger game. In particular, given a PBE of the merger game and a PBE of the cartel game, where the merged entity’s expected payoff in the merger game is less than a cartel’s expected payoff in the cartel game, then there exists a PBE of the larger game involving the same behavioral strategies and beliefs in which the firms choose to form a cartel when the cooperation state allows them to do so.

4 Results

To analyze the game, consider the stages in reverse order.

4.1 Stage 3: Post-entry bidding

Stage 3 is only reached if seller 3 has entered. Seller 3 knows whether it is competing against a merged entity, cartel, or two other noncooperative bidders.

In the high-cost state, each bidder has a cost of 1 and bids 1. The buyer pays 1 and all sellers have zero surplus.

In the low-cost state, bidding is as in a standard IPV first-price procurement (with asymmetric bidders if sellers 1 and 2 merged or formed a cartel). Given our environment, this equilibrium exists and is unique.\footnote{See, e.g., Athey (2001), Bajari (2001), and Lebrun (1996, 1999).} Let $P_{nc}$ be the expected winning bid in the low-cost state when bidders are noncooperative and $P_m$ be the expected winning bid in the low-cost state when bidders 1 and 2 have merged or formed a cartel. (The expected winning bid in Stage 3 is the same for a buyer facing a merged entity and one facing a cartel.) Note that $P_m > P_{nc}$. Let $\pi_{nc}$ be the expected surplus to one of three symmetric noncooperative bidders in the low-cost state, and let $\pi_m$ be the expected surplus to the merged entity or cartel competing against a third bidder in the low-cost state.

In what follows, to avoid uninteresting cases in which the buyer never qualifies seller 3, we assume that $k < 1 - P_m$. If $k$ is greater than $1 - P_m$, then the buyer prefers to accept the maximum bid of 1 in Stage 1 rather than move to Stage 3, where the buyer’s expected payment is at most $P_m$.

\footnote{A Perfect Bayesian Equilibrium, Bayes’ Rule is applied even following histories that have probability zero in equilibrium and so the buyer’s belief on the low-cost state conditional on observing merged firms is $\rho$, the prior probability of the low-cost state. See Fudenberg and Tirole (1991, p.332, condition B(ii)).}
4.2 Stage 2: Evaluation of bids

Whether the buyer invites seller 3 to enter depends upon whether the firms merged in Stage 0, the reprocurement cost \( k \), and the buyer’s inferences from the observed bids regarding the cost state and collusion.

In the merger game, a bid less than or equal to \( P_m + k \) is accepted because the buyer can do no better in expectation through reprocurement.\(^{33}\) A bid greater than \( P_m + k \) but less than 1 is rejected if it leads to the inference that the cost state is low because then the buyer can do better in expectation through reprocurement.

It remains to consider the buyer’s response to a bid of 1. If the buyer rejects a bid of 1, its expected payment is \( P_m \) or 1 depending on whether the cost state is low or high. Thus, the buyer is indifferent between accepting and rejecting the bid of 1 if

\[
\Pr (\text{low cost} \mid b_m = 1) P_m + (1 - \Pr (\text{low cost} \mid b_m = 1)) + k = 1.
\]

Solving this for \( k \), we get

\[
k = \Pr (\text{low cost} \mid b_m = 1) (1 - P_m).
\]

We let \( \alpha_m(k) \) denote the probability with which the buyer accepts the Stage-1 bid by a merged entity. Clearly, if \( k > \Pr (\text{low cost} \mid b_m = 1) (1 - P_m) \), then the buyer’s best response is to accept the bid, so \( \alpha_m(k) = 1 \). Similarly, if \( k < \Pr (\text{low cost} \mid b_m = 1) (1 - P_m) \), then \( \alpha_m(k) = 0 \). Thus, it will be useful to define two threshold values for \( k \), denoted \( k_m \) and \( \bar{k}_m \), where the buyer rejects a bid of 1 if \( k \leq k_m \), uses the randomized strategy of accepting a bid of 1 with probability \( \alpha_m(k) \in (0, 1) \) if \( k \in (k_m, \bar{k}_m) \), and always accepts a bid of 1 if \( k \geq \bar{k}_m \).

In the cartel game, we focus on equilibria in which noncooperative firms always bid less than 1 in the low-cost state. In this case, if the buyer observes that both bids are equal to 1, it believes it is facing either a cartel in the low-cost state or it is facing bidders in the high-cost state. The buyer is indifferent between accepting and rejecting a bid of 1 if

\[
\Pr (\text{low cost and cartel} \mid b_1 = b_2 = 1) P_m + (1 - \Pr (\text{low cost and cartel} \mid b_1 = b_2 = 1)) + k = 1,
\]

where the left side is the buyer’s expected cost if it rejects the bids, and the right side is the

\(^{33}\)Given that we allow continuous bidding increments, there is no equilibrium in which the buyer rejects a bid of \( P_m + k \) because then the merged entity’s best response would be to bid arbitrarily close to but less than \( P_m + k \).
buyer’s cost if it accepts a bid of 1. Solving this for \( k \), we get

\[
k = \Pr(\text{low cost and cartel} \mid b_1 = b_2 = 1) (1 - P_m).
\]

(2)

As with the case of a merged entity, it will be useful to define two threshold values for \( k \), which we denote by \( k_c \) and \( \bar{k}_c \), where a buyer facing non-merged firms and receiving two bids of 1 rejects both bids if \( k \leq k_c \), uses the randomized strategy of accepting a randomly chosen bid with probability \( \alpha_c(k) \in (0,1) \) if \( k \in (k_c, \bar{k}_c) \) (and rejects both bids with the complementary probability), and always accepts a randomly chosen bid if \( k \geq \bar{k}_c \).

4.3 Stage 1: Initial bidding

In the initial bidding, in the low-cost state, a merged entity or cartel will never bid less than \( P_m + k \) because a bid of \( P_m + k \) is accepted with probability 1. Bids between \( P_m + k \) and 1 are rejected with probability 1. Since the maximum Stage-1 bid is 1, the payoff for a merged entity or cartel that wins in Stage 1 is at most \( 1 - \min\{c_1, c_2\} \), while the expected payoff if the bid is rejected is \( \pi_m \). Thus, in the low-cost state, a merged entity or cartel whose minimum cost draw is greater than \( 1 - \pi_m \) prefers to have its bid rejected rather than win in Stage 1 even at the maximum price of 1.

**Lemma 1** In the merger game, in any PBE involving non-weakly-dominated bids, in the low-cost state the merged entity bids \( P_m + k, 1, \) or a bid that is rejected with probability 1.

We let \( b^* \) denote a bid that signals to the buyer that the cost state is low but that firms are not prepared to submit meaningful bids at this time. In what follows, we assume that \( b^* \) is a bid less than 1, consistent with the low-cost state, but greater than \( P_m + k \).\(^{34}\) As other interpretations, the bid of \( b^* \) might represent a qualified bidder choosing not to submit a bid at all.

In the high-cost state, all bids less than 1 are weakly dominated by a bid of 1. In particular, even though bids of \( b^* \) are rejected in equilibrium, in the high-cost state a bid of \( b^* \) is weakly dominated by a bid of 1 because the bidder would have negative surplus if the bid of \( b^* \) were accepted and always has zero surplus with a bid of 1.

**Lemma 2** In any PBE involving non-weakly-dominated bids, all bidders bid 1 in the high-cost state.

\(^{34}\)To be more precise, \( b^* \) is a function of \( k \), where \( b^*(k) \in (P_m + k, 1) \), where the interval is nonempty given our assumption that \( k < 1 - P_m \). For ease of notation, we omit the conditioning on \( k \).
4.3.1 Bidding by a merged entity

In Stage 1, a merged entity has the option of bidding $P_m + k$, which is accepted by the buyer in equilibrium. Thus, the merged entity never bids less than $P_m + k$ in equilibrium. Bids greater than $P_m + k$ other than 1 are rejected by the buyer because the buyer infers the cost state is low, and prefers to reconduct the procurement at those prices.

Thus, we consider equilibria in which the merged entity will either bid $P_m + k$, 1, or $b^*$, where a bid of $P_m + k$ is accepted with probability one, a bid of 1 is accepted with probability $\alpha(k)$, and a bid of $b^*$ is rejected with probability one. We can formulate the merged entity’s bidding strategy as a function of its cost, min $\{x_1, x_2\}$, in terms of two threshold cost values, which we denote $x_m(k)$ and $\bar{x}_m(k)$, as follows:

$$b_m(x) \equiv \begin{cases} 
P_m + k, & \text{if } x < x_m \\
1, & \text{if } x_m \leq x \leq \bar{x}_m \\
b^*, & \text{otherwise,} 
\end{cases}$$

(3)

where we suppress the conditioning of $x_m$ and $\bar{x}_m$ on $k$ for ease of notation.

Given this bidding strategy, we can define the buyer’s posterior beliefs on the low cost state following a bid of 1. Let

$$\gamma_m(x) \equiv \frac{(G(\bar{x}_m) - G(x))\rho}{(G(\bar{x}_m) - G(x))\rho + 1 - \rho},$$

where $G$ denotes the cumulative distribution function for the minimum of two random variables drawn from the uniform distribution on zero to one.\(^3\)

Given the bidding strategy in (3), the buyer’s posterior belief on the low-cost state following a bid of 1 by a merged entity is

$$\Pr(\text{low cost} \mid b_m = 1) = \gamma_m(x_m).$$

We can define an equilibrium by reprocurement cost thresholds $k_m$ and $\bar{k}_m$, mixing probability $\alpha_m$, and bid function $b_m$, which is defined in terms of cost thresholds $x_m$, and $\bar{x}_m$. These must satisfy the conditions that the buyer’s accept/reject strategy is a best response given the observed bids and the buyer’s posterior belief on the cost state, and that the merged entity’s bidding strategy is a best response given the buyer’s strategy.

We characterize an equilibrium of the merger game in the following proposition.

**Proposition 1** In the merger game, there exists a PBE involving non-weakly-dominated

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\(^3\)For $x \in [0, 1]$, $G(x) = 2x - x^2$. 

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bids in which the seller uses bid function $b_m$ given in (3), where $\bar{x}_m \equiv 1 - \pi_m$ and

$$x_m(k) \equiv \begin{cases} 
  P_m + k - \pi_m, & \text{if } k \leq k_m \\
  x \text{ s.t. } k = \gamma_m(x)(1 - P_m), & \text{if } k \in (k_m, \bar{k}_m] \\
  0, & \text{otherwise,}
\end{cases}$$

and the buyer accepts a bid less than or equal to $P_m + k$, rejects a bid strictly between $P_m + k$ and 1, and accepts a bid of 1 with probability $\alpha_m$, where

$$\alpha_m(k) \equiv \begin{cases} 
  0, & \text{if } k \leq k_m \\
  \frac{P_m + k - \pi_m - x_m(k)}{1 - \pi_m - x_m(k)}, & \text{if } k \in (k_m, \bar{k}_m) \\
  1, & \text{otherwise,}
\end{cases}$$

where $\bar{k}_m \equiv \gamma_m(0)(1 - P_m)$ and $k_m$ is implicitly defined by $k_m = \gamma_m(P_m + k_m - \pi_m)(1 - P_m)$.

Proof. See Appendix A.

The equilibrium is depicted in Figure 1, which shows $x_m$, $\bar{x}_m$, and $\alpha_m$ as functions of $k$. By looking up the value of $k$ on the horizontal axis and the value of $\min\{x_1, x_2\}$ on the vertical axis, one can identify the merged entity’s equilibrium bidding strategy. It bids $P_m + k$ if the point lies below the line $x_m(k)$, it bids 1 if the point lies above $x_m(k)$ and below $\bar{x}_m$, and it bids $b^*$ if the point lies above $\bar{x}_m$.

![Figure 1: Graph of $x_m$, $\bar{x}_m$, and $\alpha_m$ as functions of $k$.](image)

As one can see from Figure 1, as $k$ increases from zero to $k_m$, the merged entity is increasingly likely to bid $P_m + k$. That is because $P_m + k$ is, obviously, increasing in $k$, so the amount the buyer is willing to pay in the first round of bidding is increasing with
As the probability that the merged entity bids 1 decreases, the buyer’s inference on the probability of the low-cost state conditional on a bid of 1 falls, until at \( k \) equal to \( k_m \), the buyer is indifferent between accepting and rejecting a bid of 1. The merged entity’s bidding strategy then maintains that indifference for \( k \) between \( k_m \) and \( \bar{k}_m \). As \( k \) increases, it is increasingly costly for the buyer to reject a bid of 1, so the range of costs for which the merged entity bids 1 must increase in order to maintain the indifference. At \( k \) equal to \( \bar{k}_m \), the merged entity is bidding 1 for all costs less than \( 1 - \pi_m \), so for \( k \) beyond that point, the buyer’s incentives tip in favor of always accepting a bid of 1.

To focus on the buyer’s beliefs, note that the cost to the buyer of qualifying seller 3 is \( k \), and the expected benefit to the buyer from qualifying seller 3 when the Stage 1 bid is 1 is a decrease in price from 1 to \( P_m \) when the cost state is low. For \( k \in (k_m, \bar{k}_m) \), the buyer is indifferent between accepting and rejecting a bid of 1 and so it is a best response for the buyer to randomize.

### 4.3.2 Bidding by nonmerged firms

Similar to the case of a merged entity, in the cartel game there exists an equilibrium in which cartel firms submit identical bids according to the following bid function evaluated at \( \min\{x_1, x_2\} \):\(^{36}\)

\[
b_c(x) \equiv \begin{cases} 
P_c + k, & \text{if } x < x_c \\ 1, & \text{if } x_c \leq x \leq \bar{x}_c \\ b^*, & \text{otherwise.} \end{cases}
\]  

(4)

The analysis is analogous to the case of the merged entity, except that the buyer’s beliefs on the low cost state following bids of 1 must take into account the probability of a cartel. To define the beliefs, let

\[
\gamma_c(x) \equiv \frac{(G(\bar{x}_c) - G(x))\xi \rho}{(G(\bar{x}_c) - G(x))\xi \rho + 1 - \rho}.
\]

Given the bidding strategy in (4), the buyer’s posterior belief on the low-cost state following bids of 1 by nonmerged firms is

\[
\Pr(\text{low cost} \mid b_1 = b_2 = 1) = \gamma_c(x_c).
\]

We characterize an equilibrium of the cartel game in the following proposition.

\(^{36}\)In the equilibrium we consider, there is no incentive for the cartel to use one of its bids to attempt to disguise its presence. For environments in which this may be the case, see Graham and Marshall (1987) and Graham, Marshall, and Richard (1996).
Proposition 2 In the cartel game, there exists a PBE involving non-weakly-dominated bids in which noncooperative firms bid less than 1 in the low-cost state, a cartel uses bid function $b_c$ given in (4), where $\bar{x}_c \equiv 1 - \pi_m$ and

$$x_c(k) \equiv \begin{cases} P_m + k - \pi_m, & \text{if } k \leq k_c \\ x \text{ s.t. } k = \gamma_c(x)(1 - P_m), & \text{if } k \in (k_c, \bar{k}_c) \\ 0, & \text{otherwise,} \end{cases}$$

and the seller accepts the lowest bid if it is less than or equal to $P_c + k$, rejects all bids if the lowest is strictly between $P_c + k$ and $P_m + k$, accepts one bid if both are equal to $P_m + k$, rejects all bids if the lowest is strictly between $P_m + k$ and 1, and accepts one bid if both are equal to 1 with probability $\alpha_c$ (rejecting both with probability $1 - \alpha_c$), where

$$\alpha_c(k) \equiv \begin{cases} 0, & \text{if } k \leq k_c \\ \frac{P_m + k - \pi_m - x_c(k)}{1 - \pi_m - x_c(k)}, & \text{if } k \in (k_c, \bar{k}_c) \\ 1, & \text{otherwise,} \end{cases}$$

where $\bar{k}_c \equiv \gamma_c(0)(1 - P_m)$ and $k_c$ is implicitly defined by $k_c = \gamma_c(P_m + k_c - \pi_m)(1 - P_m)$.

Proof. See Appendix A.

The equilibria for the cases of merged and nonmerged firms are similar. However, the key difference is that the posterior beliefs following the observation of bids of 1 differ. For the case of nonmerged firms, bids of 1 could be the result of high costs by a cartel, high costs by noncooperative bidders, or possibly a low-cost cartel attempting to pool with the high-cost bidders. Because the cartel has the possibility to pool with high-cost noncooperative firms as well as high-cost cartels, the posterior belief on costs being low following the observation of bids of 1 is lower in the case of nonmerged firms than in the case of merged firms. That means that the buyer is more likely to accept bids of 1 made by nonmerged firms than a bid of 1 made by a merged firm.

4.4 Stage 0: Cartel versus merger

Consider Stage 0, during which the industry structure for the suppliers is determined. If the state is such that coordination is possible, firms 1 and 2 decide whether to merge or form a cartel.

We can now state our main results. Firms at least weakly prefer to form a cartel rather than merge and strictly prefer to form a cartel rather than merge for a range of reprocurement
costs. For reprocurement costs less than $k_c$, the buyer always rejects a bid of 1, regardless of whether firms are merged or not, so there is no benefit to cartel over merger. Similarly, for reprocurement costs greater than $\bar{k}_m$, the buyer always accepts a bid of 1, so again there is no benefit to cartel over merger. However, for $k \in (k_c, \bar{k}_m)$, firms have strictly greater expected payoff as a cartel than as a merged entity. In this range, the buyer accepts bids of 1 from nonmerged firms with greater probability than from a merged entity. Intuitively, a buyer facing nonmerged firms places some probability weight on bids of 1 coming from noncooperative firms in the high-cost state, in which case the buyer prefers to accept one of the bids.

**Proposition 3** There exist PBEs involving non-weakly-dominated bids for the merger game and cartel game such that for all $k$, a cartel with cost draws $x_1$ and $x_2$ has weakly greater expected payoff from the perspective of Stage 1 than does a merged entity with the same cost draws, and strictly greater for $k \in (k_c, \bar{k}_m)$.

The comparison between merger and cartel is depicted in Figures 2 and 3 for the two different possible orderings of $k_m$ and $\bar{k}_c$, where the case of Figure 2 with $k_m > \bar{k}_c$ holds for $\xi$ sufficiently small. As shown in the figures, for $k \in (k_c, \bar{k}_m)$, for any cost draws by the firms, the expected payoff is greater as a cartel than as a merged entity. This implies that for any prior distribution on the buyer’s reprocurement costs with support $(0, 1 - P_m)$, firms strictly prefer to collude rather than merge when the coordination state allows that.

![Figure 2: Illustration of equilibria for sufficiently low $\xi$.](image)

As we have demonstrated above, a cartel is better able to exploit the buyer’s uncertainty about the state to successfully submit high bids when in the low-cost state. Additional uncertainty about the existence of a cartel leads the buyer to be more lenient in terms of accepting higher prices relative to when it faces a merged entity. Stated differently, a
merged entity faces greater buyer resistance than firms operating as a cartel when the buyer is uncertain as to whether the firms are in a cartel or acting noncooperatively.

4.5 Equilibrium selection

With regard to the multiplicity of equilibria, under a restriction on beliefs, as long as the probability of the cooperation state that allows collusion is sufficiently small, the sellers prefer to collude rather than merge regardless of the equilibrium selection. Intuitively, it must be sufficiently likely that sellers are noncooperative in order for the sellers to benefit from pooling with them regardless of the equilibrium selection.

Recall that Lemma 1 shows that a merged entity will bid only $P_m + k$, 1, or a bid that is rejected with probability one in equilibrium. A similar result to Lemma 1 is available for the cartel game, except one must specify that the buyer believes identical bids (other than $b^*$) come from a cartel. In the absence of this assumption, there is an equilibrium in which the cartel bids $P_{nc} + k$ (rather than $P_m + k$), 1, or $b^*$, supported by the beliefs that any bids greater than $P_{nc} + k$ and less than 1, including $P_m + k$, come from noncooperative bidders, making it a best reply for the buyer to reject those bids.

**Definition 1** An equilibrium of the cartel game has suspicious beliefs if the buyer believes different bids come from noncooperative bidders and identical bids less than or equal to $P_m + k$ come from a cartel.

With this restriction on beliefs, the cartel game also has the feature that the cartel bids only $P_m + k$ or 1 or bids that are rejected with probability 1.
Lemma 3 In the cartel game, in any PBE involving non-weakly-dominated bids and suspicious beliefs, in the low-cost state the cartel submits identical bids equal to $P_m + k$ or 1 or submits bids that are rejected with probability 1.

Proof. See Appendix A.

It follows from Lemma 1 that in the merger game, given a PBE involving non-weakly-dominated bids, when the buyer’s acceptance function is $\alpha$, a merged entity with minimum cost draw $x$ has expected payoff

$$\max \{P_m + k - x, \, \alpha(1 - x) + (1 - \alpha)\pi, \, \pi \}$$

which is nondecreasing in $\alpha$. Thus, an equilibrium that involves a greater probability of buyer acceptance offers at least weakly greater expected payoff to the merged entity. Because of this, we can identify the “best” equilibrium of the merger game for the merged entity, i.e., the equilibrium that gives the merged entity the greatest expected payoff, by identifying the equilibrium with the greatest probability of buyer acceptance.

Similarly, using Lemma 3, we can identify the “worst” equilibrium for the cartel in the cartel game. The worst cartel equilibrium differs from the one previously identified in that in some cases a cartel with costs greater than $1 - \pi_m$ bids 1 rather than $b^*$. This increases the buyer’s posterior belief on the low-cost state following a bid of 1 and shifts the buyer’s response towards rejecting bids of 1. By doing this to the maximal extent possible, i.e., by having the cartel bid 1 when its cost is greater than $1 - \pi_m$ whenever bids of 1 are rejected with probability 1, we can construct the worst equilibrium for the cartel.

We conclude by showing that for $\xi$ sufficiently small, the worst cartel equilibrium is better for the sellers than the best merger equilibrium.

Proposition 4 Focusing on PBE involving non-weakly-dominated bids, noncooperative bids less than 1 in the low-cost state, and suspicious beliefs, for all $\rho \in (0, 1)$, there exists $\bar{\xi} > 0$ such that $\forall \xi < \bar{\xi}$, for all $k$, the best equilibrium outcome for the seller in the merger game gives weakly lower expected payoff than than the worst equilibrium outcome for the cartel in the cartel game, with strictly lower expected payoff for a nonempty range of reprocurement costs.

Proof. See Appendix A.
We conclude that even when one considers the issue of multiplicity of equilibria, for reasonable parameter values the expected payoff from forming a cartel exceeds the expected payoff from merging in an environment such as ours with buyer resistance.

4.6 Immediate qualification of seller 3

In our model, it is not a choice for the buyer to immediately qualify seller 3; however, that option can be introduced. In one possible alternative extensive form, if the buyer immediately qualifies seller 3, then it holds a single auction, buying at the lowest bid. In this extensive form, the buyer at least weakly prefers to consider bids from sellers 1 and 2 before potentially qualifying seller 3.

In another alternative extensive form, if the buyer qualifies seller 3 immediately at cost \( k \), then it continues to have the option to reject the bids in the first procurement and reconduct the procurement at no additional cost. In that case, the buyer is able to, in effect, sample six cost draws rather than only five as in our model, which may give the buyer an incentive to immediately qualify seller 3. Nevertheless, in this version of the model, one would expect the same forces to favor cartel over merger, although the ability of either to successfully bid 1 in the low-cost state would be dampened by the presence of seller 3 in the first-stage procurement.

4.7 Cartel detection

In our model a cartel has no incentive to try to disguise its presence other than using bids that mimic bids in the high-cost state. In the case of nonmerged firms, bids of \( P_m + k \) in Stage 1 allow the inference of collusion. In addition, Stage 3 bids that are less than 1 when the Stage 1 bids were equal to 1 also allow the inference of collusion. If a cartel faced penalties from detection, either from legal enforcement or from lost future profits due to increased buyer resistance in the future (for example, the equilibrium might revert to that associated with a merged entity), then that would affect cartel behavior.

Suppose that such penalties only apply if the observed behavior allows the inference of collusion with probability one. Then cartel firms would have an incentive to randomize over a region below \( P_{nc} + k \) rather than bid \( P_m + k \), and low-cost cartel firms would bid 1 in Stage 1 for a smaller range of costs. In addition, low-cost cartel firms would never bid 1 when bids of 1 are always rejected. Nevertheless, an equilibrium similar to the one we constructed continues to exist, although it requires an adjustment to the noncooperative bidding strategy.

In the equilibrium we construct for nonmerged firms, when \( k < k_c \), noncooperative firms bid \( b^* \) when they prefer that their bid be rejected. However, since bids of 1 are also rejected
when $k < k_c$, it would also be a best reply for them to bid 1. If cartel firms do not bid 1 when $k < k_c$, then in order to maintain the buyer’s incentive to reject bids of 1, low-cost noncooperative firms must bid 1 for some costs. (To see this, note that if low-cost bidders never bid 1, then the buyer’s inference from bids of 1 would be that costs are high, and so the buyer would prefer to accept one of the bids.) With the required adjustment to the noncooperative bidding strategy for low reprocurement costs, we retain the result that, as long as penalties for collusion are not too severe, low-cost cartels will sometimes bid 1, pooling with high-cost bidders.

5 Merger efficiencies

The U.S. Horizontal Merger Guidelines state that “a primary benefit of mergers to the economy is their potential to generate significant efficiencies.” In order to allow for efficiencies associated with a merger, we consider the extreme case in which merging firms have a cost of zero in the low-cost state, while continuing to have a cost of one in the high-cost state.

In equilibrium, the merger with extreme efficiencies bids 1 in the high-cost state and in the low-cost state mixes between the largest bid that is accepted with probability one and a bid of one for low values of $k$ and bids one for high values of $k$. The buyer mixes between accepting and rejecting a bid of one for low values of $k$ and accepts a bid of one for high values of $k$. In the event of a reprocurement in the low-cost state, the equilibrium bid strategies of the merged entity and seller 3 are as calculated in Vickrey (1961, Appendix III).

For a formal statement of the equilibrium, see Appendix B.

We can now compare the expected payoffs of a merged entity with no efficiencies, a merged entity with extreme efficiencies, and a cartel. As you can see from Figure 4, which assumes $\rho = 0.75$ and $\xi = 0.1$, for a substantial range of possible values of $k$, the expected payoff from cartel exceeds that from a merger even with extreme efficiencies.

For these parameter values, there exists a range of values for $k$ around $k = 0.1$ for which the cartel payoff is over 70% more than the merger payoff and the cartel payoff is more than 55% more than the payoff for a merger with extreme efficiencies. We conclude from Figure 4 and related calculations that the value to a clandestine cartel in terms of reduced buyer resistance relative to merger is sufficiently large that it can outweigh even significant merger efficiencies.

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When authorities take away collusion as an option, firms may turn to merger as a second-best option. For example, as discussed in Section 2, there are many examples of mergers, acquisitions, and joint ventures among firms that were found by the European Commission to have engaged in collusion. These transactions typically do not involve all of the firms that were involved in the conspiracy, which may suggest another advantage of clandestine cartel over merger, namely that it allows the suppression of rivalry among a larger number of firms than would have been permitted through a merger. However, the evidence from the industrial merger wave of 1898 to 1904 suggests that there is a benefit to forming a clandestine cartel even when compared to a merger among all of the firms in an industry.\textsuperscript{38}

\section{Conclusion}

It might seem that a merged entity should be able to do anything that a cartel can do, plus more, and so should earn higher profits than a cartel. But in the late 1800s, when firms were relatively unencumbered in the choice between merging or forming a cartel, many chose to function as a cartel. In a review of recent cartel cases at the European Commission, a substantial number of cartel cases are followed by mergers or joint ventures by a subset of firms.

\textsuperscript{38}See Waehrer (1999) on incentives for firms to form smaller versus larger merged entities and Waehrer and Perry (2003) on incentives for only a subset of firms in an industry to merge in environments with strategic buyers.
the colluding firms.

Whereas a merger is a publicly observed event, a cartel is a clandestine operation. Other noncartel firms in an industry may be aware of the existence of a cartel, but the buyers that procure from colluding firms are usually uncertain of the existence of the cartel. In a model that parallels buyer procurement practices as well as the informational environment that confronts procurement participants, we show that a cartel can hide behind the possibility that their members might be noncooperative bidders to enhance their profits relative to a merged entity.

Our model suggests that the incremental profits available to firm from collusion rather than merger can be substantial and can outweigh even significant merger efficiencies.

In our model, the buyer can invoke additional competitive pressure by inviting a new firm to bid in a reconducted procurement. In practice, reserving the right to void a procurement and resolicit bids is commonplace.

Overall, our analysis highlights the importance of accounting for strategic action by buyers during the procurement process. In practice, buyers are not passive but, rather, actively evaluate the competitive process during a procurement and make profit-enhancing adjustments to increase the policing function of competition as deemed appropriate.
Appendix: Proofs

Proof of Proposition 1. Let the buyer believe the cost state is low if it observes a bid less than 1, and let the buyer believe the cost state is low with probability $\gamma_m(x_m)$ when the bid is 1. This belief is consistent with Bayes’ Rule given the merged entity’s bidding strategy $b_m$. The definitions of $x_m$ and $\bar{x}_m$ are such that the buyer’s strategy is a best response. The definition of $\alpha_m$ is such that the merged entity’s strategy is a best response. First consider the buyer’s accept/reject strategy. For $k \leq k_m, \alpha_m(k) = 0$, for $k \geq \bar{k}_m, \alpha_m(k) = 1$, and for $k \in (k_m, \bar{k}_m)$, the buyer strictly mixes between accepting and rejecting bids of 1 and so must be indifferent. Using (1), this requires:

$$\forall k \in (k_m, \bar{k}_m), k = \gamma(x_m(k))(1 - P_m), \quad (A.1)$$

with the left side being weakly less for $k \leq k_m$ and weakly more for $k \geq \bar{k}_m$. The optimality of the merged entity’s bidding strategy requires that

$$\forall x \leq x_m(k), P_m + k - x \geq \max \{\pi_m, (1 - x)\alpha_m(k) + \pi_m(1 - \alpha_m(k))\}$$
$$\forall x \in (x_m(k), \bar{x}_m(k)], (1 - x)\alpha_m(k) + \pi_m(1 - \alpha_m(k)) \geq \max \{\pi_m, P_m + k - x\}$$
$$\forall x > \bar{x}_m(k), \pi_m \geq \max \{P_m + k - x, (1 - x)\alpha_m(k) + \pi_m(1 - \alpha_m(k))\}.$$ 

One can show that these conditions are satisfied at the values defined in Proposition 1. In addition, one can confirm that $0 \leq x_m \leq \bar{x}_m \leq 1$ and $\alpha \in [0, 1]$. Q.E.D.

Proof of Proposition 2. The proof is analogous to that of Proposition 1 with the addition that one must specify the bidding strategy of noncooperative firms and buyer beliefs regarding the existence of a cartel. As described further below, there exists an equilibrium in which each noncooperative firm bids according to the equilibrium noncooperative bid function associated with a sealed-bid procurement with a reserve price $P_{nc} + k$ and an outside option of $\pi_{nc}$. In that case, a firm with cost zero bids a positive amount less than $P_{nc} + k$ and a firm with cost $P_{nc} + k - \pi_{nc}$ bids $P_{nc} + k$, with continuously increasing bids for intermediate costs. Noncooperative firms with costs greater than $P_{nc} + k - \pi_{nc}$ bid $b^*$. The equilibrium is supported by beliefs such that if the buyer observes at least one bid less than 1, then the buyer believes the cost state is low. If the buyer observes at least one bid not equal to $P_m + k$, 1, or $b^*$, then the buyer believes it is facing noncooperative bidders with probability

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39 If $b^*$ is not defined as a bid less than 1, then the buyer would also believe the cost state is low when it observes $b^*$.

40 In extensions in which $b^*$ is not defined as a bid less than 1, then the buyer would also believe the cost state is low when it observes at least one bid of $b^*$.
one. If the buyer observes both bids equal to $P_m + k$, the buyer believes it is facing a cartel with probability one. If the buyer observes that both bids are equal to $\beta_\text{m}$, then the buyer’s beliefs are determined by Bayes’ Rule and given by $\gamma_c(x_c(k))$. If the buyer observes that both bids are equal to $1$, its beliefs are determined by Bayes’ Rule and given by $\gamma_c(x_c(k))$. If the buyer observes that both bids are equal to $b^*$, then the buyer’s beliefs are determined by Bayes’ Rule, but given that $b^* > P_m + k$, regardless of the belief, the buyer’s best response is to reject the bids.

The bid function for a noncooperative bidder with cost $x$ is given by

$$\beta_{nc}(x, k) = \begin{cases} \tilde{\beta}(x), & \text{if } x \leq P_{nc} + k - \pi_{nc} \\ b^*, & \text{otherwise}, \end{cases}$$

where $\tilde{\beta}(x) \equiv \frac{1}{2(1-x)} (2(P_{nc} + k)(1 - x_{nc}(k)) + (x_{nc}(k)^2 - x^2))$, which satisfies $\tilde{\beta}(P_{nc} + k - \pi_{nc}) = P_{nc} + k$. This bid function has the feature that a noncooperative bidder with cost $P_{nc} + k - \pi_{nc}$ is indifferent between bidding $\tilde{\beta}(P_{nc} + k - \pi_{nc})$ and winning with probability $1 - F(P_{nc} + k - \pi_{nc})$ and bidding $b^*$ and receiving an expected payoff of $\pi_{nc}$ in the next stage with probability $1 - F(P_{nc} + k - \pi_{nc})$. Noncooperative bidders with lower costs strictly prefer to bid according to $\tilde{\beta}$ rather than bid $b^*$, and noncooperative bidders with higher costs strictly prefer to bid $b^*$. Given the buyer’s beliefs, and given that the other noncooperative firm either bids less than or equal to $P_{nc} + k$ or bids $b^*$, a deviant bid by a noncooperative firm (i.e., greater than $P_{nc} + k$ and not equal to $b^*$) does not change the buyer’s inference that costs are low and bidders are noncooperative. Thus, such deviant bids are not profitable. The remainder of the proof is analogous to that of Proposition 1. Q.E.D.

**Proof of Proposition 3.** To analyze Stage 0, as a preliminary result, consider the four thresholds for the buyer’s repurchase cost defined in Propositions 1 and 2. Given $\rho$, there exists $\tilde{\xi} > 0$ such that for all $\xi < \tilde{\xi}$ the repurchase cost thresholds satisfy $0 < k_c < \tilde{k}_c < k_m < \tilde{k}_m < 1 - P_m$ and for $\xi > \tilde{\xi}$ they satisfy $0 < k_c < k_m < \tilde{k}_c < \tilde{k}_m < 1 - P_m$. To see this, note that it is straightforward to show that all the thresholds are in the interval $(0, 1 - P_m)$ and that $k_m < \tilde{k}_m, k_c < \tilde{k}_c, k_c < k_m, \text{ and } \tilde{k}_c < \tilde{k}_m$. The result for $\tilde{\xi}$ follows the facts that $k_m$ is positive and does not depend on $\xi$ and $\tilde{k}_c$ is strictly increasing in $\xi$. The comparison of payoffs for cartel versus merger follows from a comparison of $\alpha_m$ and $\alpha_c$.

Q.E.D.

**Proof of Lemma 3.** First, if the buyer observes identical bids less than $P_m + k$, then by the assumption of suspicious beliefs the buyer believes the bids come from the cartel in the low-cost state (using Lemma 2) and so the buyer accepts one of the bids. Because the buyer accepts all identical bids less than $P_m + k$, no bids less than $P_m + k$ are a best response.
by the cartel because the cartel would have greater expected payoff by submitting identical bids for a slightly higher amount that remains less than $P_m + k$. Thus, in equilibrium the buyer accepts identical bids of $P_m + k$. Second, bids greater than $P_m + k$ and less than 1 are rejected with probability one because, given Lemma 2, the buyer infers that the cost-state is low and so strictly prefers to reject the bids. It follows that in equilibrium the cartel submits identical bids equal to $P_m + k$, identical bids equal to 1, or bids such that both bids are rejected with probability 1. Q.E.D.

**Proof of Proposition 4.** For $\xi$ sufficiently small, by Lemma 2, we can order the reprocurement cost thresholds as $\hat{k}_e < \tilde{k}_e < k_m < \tilde{k}_m$. For $k \leq k_m$, $\hat{\alpha}_c(k) \geq \alpha_m(k) = 0$ and for $k \geq \tilde{k}_e$, $\hat{\alpha}_c(k) = 1 \geq \alpha_m(k)$. Thus, for all $k$, $\hat{\alpha}_c(k) \geq \alpha_m(k)$, with a strict inequality for $k \in (\hat{k}_c, k_m)$. The result then follows from Lemmas A.1 and A.2 below. Q.E.D.

**Lemma A.1** In the merger game, the equilibrium with acceptance probability $\alpha_m$ provides the merged entity with the greatest expected payoff among all PBE involving non-weakly-dominated bids.

**Proof of Lemma A.1.** To prove the result, we show that in the merger game, in any PBE involving non-weakly-dominated bids, given $k$, the probability that the buyer accepts a bid of 1 is less than or equal to $\alpha_m(k)$.

For $k \geq \tilde{k}_m$, the result follows from $\alpha_m(k) = 1$. Let $k < \tilde{k}_m$. Suppose an equilibrium acceptance probability $\alpha > \alpha_m(k)$. One can show that $k < \tilde{k}_m$ implies $\alpha < 1$.\(^1\) Using Lemma 1, the merged entity bids 1 if $x \in \left(\frac{P_m + k - \alpha}{1 - \alpha} - \pi_m, 1 - \pi_m\right)$, but not if $x < \frac{P_m + k - \alpha}{1 - \alpha} - \pi_m$ or if $x > 1 - \pi_m$. Letting $\gamma$ be the buyer’s posterior belief on the low-cost state following a bid of 1 and using Lemma 2, it follows that

$$\gamma(1 - P_m) = \frac{(G(1 - \pi_m) - G\left(\frac{P_m + k - \alpha}{1 - \alpha} - \pi_m\right)) \rho}{(G(1 - \pi_m) - G\left(\frac{P_m + k - \alpha}{1 - \alpha} - \pi_m\right)) \rho + 1 - \rho(1 - P_m)}$$

$$= \gamma_m \left(\frac{P_m + k - \alpha}{1 - \alpha} - \pi_m\right)(1 - P_m)$$

$$> \gamma_m(x_m(k))(1 - P_m)$$

$$\geq k,$$

where the first equality uses Bayes’ Rule, the second equality uses the definition of $\gamma_m$, the inequality uses the definition of $\alpha_m(k)$, which implies $x_m(k) = \frac{P_m + k - \alpha_m(k)}{1 - \alpha_m(k)} - \pi_m$ and

\(^1\)If $\alpha = 1$, then the merged entity’s best response is to bid 1 for all $x < 1 - \pi_m$ and not for $x > 1 - \pi_m$, which implies a posterior belief of $\gamma_m(0)$. But $\gamma_m(0)(1 - P_m) = \tilde{k}_m > k$, which implies the buyer strictly prefers to reject a bid of 1, contradicting $\alpha = 1$. 

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α > α_m(k), and the final equality uses for k ∈ (k_m, k̈_m) the definition of x_m(k), which implies γ_m(x_m(k)) (1 − P_m) = k, and for k ≤ k_m uses α_m(k) = 0, which implies γ_m(x_m(k)) (1 − P_m) ≥ k. The implied inequality γ(1 − P_m) > k implies the buyer strictly prefers to reject a price of 1, contradicting α > 0. Q.E.D.

Lemma A.2 In the cartel game, the equilibrium with acceptance probability α_c, where

\[
\hat{\alpha}(k) = \begin{cases} 
0, & \text{if } k \leq \hat{k}_c \\
\text{s.t. } P_m + k - x_c(k) = (1 - x_c(k))\hat{\alpha} + \pi_m(1 - \hat{\alpha}), & \text{if } k \in (\hat{k}_c, \bar{k}_c) \\
1, & \text{if } k \geq \bar{k}_c 
\end{cases}
\]

and \(\hat{k}_c \in (k_c, \bar{k}_c)\) is defined

\[
\hat{k}_c = \frac{(1 - G(P_m + \hat{k}_c - \pi_m))\xi\rho}{(1 - G(P_m + \hat{k}_c - \pi_m))\xi\rho + 1 - \rho}(1 - P_m),
\]

by provides the cartel with the least expected payoff among all PBE involving non-weakly-dominated bids, noncooperative bids less than 1 in the low-cost state, and suspicious beliefs.

Proof of Lemma A.2. To prove the result, we show that in the cartel game, in any equilibrium satisfying the conditions of the proposition, for all k, the probability that the buyer accepts a bid of 1 is greater than or equal to \(\hat{\alpha}_c(k)\).

For k ≤ \(\hat{k}_c\), the result follows from \(\hat{\alpha}_c(k) = 0\). Let k > \(\hat{k}_c\). Suppose an equilibrium acceptance probability α < \(\hat{\alpha}_c(k)\), which implies α < 1. Using Lemma 3, the cartel bids 1 if \(x \in \left(\frac{P_m + k - \alpha}{1 - \alpha} - \pi_m, 1 - \pi_m\right)\), but not if \(x < \frac{P_m + k - \alpha}{1 - \alpha} - \pi_m\) or if \(x > 1 - \pi_m\). Letting γ be the buyer’s posterior belief on the low-cost state following a bid of 1 and using Lemma 2 and the assumption of noncooperative bids less than 1 in the low-cost state, it follows that

\[
\gamma(1 - P_m) = \frac{(G(1 - \pi_m) - G\left(\frac{P_m + k - \alpha}{1 - \alpha} - \pi_m\right))\xi\rho}{(G(1 - \pi_m) - G\left(\frac{P_m + k - \alpha}{1 - \alpha} - \pi_m\right))\xi\rho + 1 - \rho}(1 - P_m)
\]

\[
= \gamma_c \left(\frac{P_m + k - \alpha}{1 - \alpha} - \pi_m\right)(1 - P_m)
\]

\[
< \gamma_c(x_c(k))(1 - P_m)
\]

\[
\leq k,
\]

where the first equality uses Bayes’ Rule, the second equality uses the definition of γ_c, the inequality uses the definition of \(\hat{\alpha}_c(k)\), which implies \(x_c(k) = \frac{P_m + k - \hat{\alpha}_c(k)}{1 - \hat{\alpha}_c(k)} - \pi_m\) and α < \(\hat{\alpha}_c(k)\), and the final equality uses for k ∈ (\(\hat{k}_c, \bar{k}_c\)) the definition of x_c(k), which implies
\( \gamma_c(x_c(k))(1 - P_m) = k \), and for \( k \geq \bar{k}_c \) uses \( \hat{\alpha}_c(k) = 1 \), which implies \( \gamma_c(x_c(k))(1 - P_m) \leq k \).

The implied inequality \( \gamma(1 - P_m) < k \) implies the buyer strictly prefers to accept a price of 1, contradicting \( \alpha < 1 \). Q.E.D.

**B Appendix: Equilibrium with extreme efficiencies**

Modify the merger game so that a merged entity has cost of zero in the low-cost state and continues to have a cost of one in the high-cost state.

In the event of a reprocurement in the low-cost state with the merged entity bidding against seller 3, the results of Vickrey’s (1961) Appendix III for the Dutch Auction (with \( a = 1 \) in Vickrey’s notation to correspond to a cost of zero in a procurement) imply that the merged entity’s expected payment is \( \frac{1}{2} \) and its expected surplus is \( \pi_{mm} \equiv \frac{1}{4} \). Vickrey’s results also imply that the buyer has an expected payment from reprocurement in the low-cost state of \( P_{mm} \equiv 0.324543 \).

To define the equilibrium, consider the following strategies and beliefs.

The merged entity bids 1 in the high-cost state and in the low-cost state bids according to:

\[
b_{mm} = \begin{cases} 
P_{mm} + k & \text{with prob. } 1 - \sigma \text{ and } 1 \text{ with prob. } \sigma, \\
1 & \text{otherwise},
\end{cases}
\]

where \( \sigma = \frac{k(1 - \rho)}{\rho(1 - P_{mm} - k)} \). The buyer accepts bids less than or equal to \( P_{mm} + k \), rejects bids in \( (P_{mm} + k, 1) \), and accepts a bid of 1 with probability \( \alpha_{mm} \), where

\[
\alpha_{mm} = \begin{cases} 
\frac{P_{mm} + k - \pi_{mm}}{1 - \pi_{mm}} & \text{if } k \leq \rho(1 - P_{mm}) \\
1 & \text{otherwise}.
\end{cases}
\]

The buyer’s beliefs on the low-cost state following a bid less than 1 are 1 and following a bid of 1 are:

\[
\gamma_{mm} = \begin{cases} 
\frac{k}{1 - P_{mm}} & \text{if } k \leq \rho(1 - P_{mm}) \\
\rho & \text{otherwise},
\end{cases}
\]

which one can show follows from Bayes’ Rule given the bid strategies.

One can show that these strategies and beliefs form an equilibrium.

Given the beliefs, the buyer is maximizing its expected payoff. If it accepts a bid of \( b < 1 \), it pays \( b \), but if it rejects that bid, it expects to pay \( P_{mm} + k \). If the buyer accepts a bid of
1, it pays 1, but if it rejects that bid, it expects to pay

$$\gamma_{mm} P_{mm} + (1 - \gamma_{mm}) + k.$$ 

For $$k \leq \rho(1 - P_{mm})$$, we have

$$\gamma_{mm} P_{mm} + (1 - \gamma_{mm}) + k = 1,$$

so the buyer is indifferent. For $$k > \rho(1 - P_{mm})$$,

$$\gamma_{mm} P_{mm} + (1 - \gamma_{mm}) + k = 1 - \rho(1 - P_{mm}) + k < 1,$$

so the buyer prefers to accept.

Given the buyer’s strategy, the merged entity maximizes its expected payoff because for $$k \leq \rho(1 - P_{mm})$$, the merged entity’s payoff if it wins with a bid of $$P_{mm} + k$$ is equal to its expected payoff if it bids 1, which is $$\alpha_{mm} + (1 - \alpha_{mm})\pi_{mm}$$. To see this, note that

$$\alpha_{mm} + (1 - \alpha_{mm})\pi_{mm} = \frac{P_{mm} + k - \pi_{mm}}{1 - \pi_{mm}} + \left(1 - \frac{P_{mm} + k - \pi_{mm}}{1 - \pi_{mm}}\right)\pi_{mm} = P_{mm} + k.$$ 

If $$k > \rho(1 - P_{mm})$$, the merged entity’s payoff if it wins with a bid of $$P_{mm} + k$$ is less than its payoff with a bid of 1 (since $$k \leq 1 - P_{mm}$$).

We can compare expected payoffs by noting that with extreme efficiencies the merged entity’s expected payoff in the low-cost state is

$$\begin{cases} 
(1 - \sigma)(P_{mm} + k) + \sigma(\alpha_{mm} + (1 - \alpha_{mm})\pi_{mm}), & \text{if } k \leq \rho(1 - P_{mm}) \\
1, & \text{otherwise.}
\end{cases}$$
Appendix For Online Publication

C.1 Appendix: Historical evidence of collusion followed by merger

We review the ten largest (in net value) manufacturing industry groups according to the U.S. census of 1900 for evidence of industries with cartels followed by mergers.\textsuperscript{42} The information provided in Table C.1 is not exhaustive. We provide representative examples of the observed phenomenon for the time period closely following the passage of the Sherman Act.

Table C.1: Evidence of the pattern of collusion followed by merger

<table>
<thead>
<tr>
<th>Census industry group</th>
<th>Industry with cartel followed by merger</th>
<th>Merger year</th>
<th>References for existence of cartel and merger year</th>
</tr>
</thead>
<tbody>
<tr>
<td>Food and kindred products</td>
<td>Meat packing</td>
<td>1903</td>
<td>Whitney (1958, vol. 1, pp.31,34)</td>
</tr>
<tr>
<td></td>
<td>Sugar refining</td>
<td>1887</td>
<td>Genesove and Mullin (1998, p.358)</td>
</tr>
<tr>
<td></td>
<td>Corn refining</td>
<td>1897</td>
<td>Whitney (1958, vol. 2, p.258)</td>
</tr>
<tr>
<td>Textiles</td>
<td>Cordage</td>
<td>1887</td>
<td>Thorelli (1954, p.78)</td>
</tr>
<tr>
<td></td>
<td>Cotton yarn</td>
<td>1899</td>
<td>Dewing (1914, pp.307-308)</td>
</tr>
<tr>
<td>Iron and steel and their products</td>
<td>Wire nails</td>
<td>1898</td>
<td>Lamoreaux (1985, pp.69-74), Jones (1921, p.194)</td>
</tr>
<tr>
<td></td>
<td>Strawboard</td>
<td>1889</td>
<td>Weeks (1916, pp.305-306)</td>
</tr>
<tr>
<td>Chemicals and allied products</td>
<td>Gun powder</td>
<td>1902</td>
<td>Whitney (1958, vol. 1, p.192)</td>
</tr>
<tr>
<td></td>
<td>Cottonseed oil</td>
<td>1889</td>
<td>Thorelli (1954, p.79)</td>
</tr>
<tr>
<td>Metals and metal products, other than iron and steel</td>
<td>Farm machinery</td>
<td>1902</td>
<td>Jones (1912, p.232)</td>
</tr>
<tr>
<td>Liquors and beverages</td>
<td>Whiskey</td>
<td>1891</td>
<td>Ripley (1916, pp.27,31)</td>
</tr>
<tr>
<td>Leather and its finished products</td>
<td>Sole leather (tanning)</td>
<td>1893</td>
<td>Dewing (1914, p.18)</td>
</tr>
<tr>
<td>Lumber and its remanufactures</td>
<td>**</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Tobacco ***</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

* Some cartel members merged with the Union Bag and Paper Co. The date is uncertain.

** In the lumber industry it was common for manufacturers to participate in price fixing associations. In at least one case the association subsequently attempted to merge, but decided against it due to legal barriers (U.S. Department of Commerce, 1914, pp.256, 274).

*** The five largest tobacco product manufacturers merged in 1890. They merged after considering and deciding against forming a cartel (Porter, 1969).

\textsuperscript{42} U.S. Census Office (1902, p.325). The Twelfth Census classified industries into fifteen groups. The industry groups absent in our sample from the Census classifications are (i) clay, glass, and stone products, (ii) vehicles for land transportation, (iii) shipbuilding, (iv) miscellaneous industries, and (v) hand trades. Our sample includes the ten most valuable groups excluding miscellaneous industries and hand trades.

\textsuperscript{43}The EC Decisions are available at http://ec.europa.eu/competition/cartels/cases/cases.html (accessed November 25, 2012). We exclude non-industrial products, such as bananas, grains and oilseeds, beer, and tobacco, banking-related cartels, SAS/Maersk Air, and Fine Art Auction Houses. We also exclude cases whose decisions do not identify the cartel participants (Cement and related products, Paper envelope, Polyurethane foam, and Smart card chips).
Table C.2: Buyer power and post-collision mergers

<table>
<thead>
<tr>
<th>EC Decision</th>
<th>Concentrated buyers</th>
<th>Fragmented buyers</th>
</tr>
</thead>
<tbody>
<tr>
<td>Carbonless Paper 20-Dec-01</td>
<td>Yes</td>
<td>No</td>
</tr>
<tr>
<td>Choline Chloride 9-Dec-04</td>
<td>Yes</td>
<td>No</td>
</tr>
<tr>
<td>Citric Acid 5-Dec-01</td>
<td>Yes</td>
<td>No</td>
</tr>
<tr>
<td>Concrete Reinforcing Bar 17-Dec-02</td>
<td>Yes</td>
<td>No</td>
</tr>
<tr>
<td>Copper Plumbing Tubes 3-Sep-04</td>
<td>Yes</td>
<td>No</td>
</tr>
<tr>
<td>Electrical and mechanical carbon and graphite products 3-Dec-03</td>
<td>Yes</td>
<td>No</td>
</tr>
<tr>
<td>Food flavour enhancers 17-Dec-02</td>
<td>Yes</td>
<td>No</td>
</tr>
<tr>
<td>Graphite electrodes 18-Jul-01</td>
<td>Yes</td>
<td>No</td>
</tr>
<tr>
<td>Industrial and medical gases 24-Jul-02</td>
<td>Yes</td>
<td>No</td>
</tr>
<tr>
<td>Industrial Bags 30-Nov-05</td>
<td>Yes</td>
<td>No</td>
</tr>
<tr>
<td>Industrial tubes 16-Dec-03</td>
<td>Yes</td>
<td>No</td>
</tr>
<tr>
<td>Methionine 2-Jul-02</td>
<td>Yes</td>
<td>No</td>
</tr>
<tr>
<td>Methylglucamine 27-Nov-02</td>
<td>Yes</td>
<td>No</td>
</tr>
<tr>
<td>Monochloroacetic Acid 19-Jan-05</td>
<td>Yes</td>
<td>No</td>
</tr>
<tr>
<td>Needles 26-Oct-04</td>
<td>Yes</td>
<td>No</td>
</tr>
<tr>
<td>Organic peroxides 10-Dec-03</td>
<td>Yes</td>
<td>No</td>
</tr>
<tr>
<td>Plasterboard 27-Nov-02</td>
<td>Yes</td>
<td>No</td>
</tr>
<tr>
<td>Rubber chemicals 21-Dec-05</td>
<td>Yes</td>
<td>No</td>
</tr>
<tr>
<td>Sodium Gluconate I 2-Oct-01</td>
<td>Yes</td>
<td>No</td>
</tr>
<tr>
<td>Sodium Gluconate II 29-Sep-04</td>
<td>Yes</td>
<td>No</td>
</tr>
<tr>
<td>Sorbates 1-Oct-03</td>
<td>Yes</td>
<td>No</td>
</tr>
<tr>
<td>Specialty Graphite 17-Dec-02</td>
<td>Yes</td>
<td>No</td>
</tr>
<tr>
<td>Thread 14-Sep-05</td>
<td>Yes</td>
<td>No</td>
</tr>
<tr>
<td>Vitamins 21-Nov-01</td>
<td>Yes</td>
<td>No</td>
</tr>
<tr>
<td>Zinc phosphate 11-Dec-01</td>
<td>Yes</td>
<td>No</td>
</tr>
<tr>
<td>Total</td>
<td>4</td>
<td>1</td>
</tr>
</tbody>
</table>

C.2 Appendix: Bid rejections and reprocurement in practice

In order to seek the best value when acquiring products or services, firms typically use competitive procurements. Governments, whether local, state or federal, are typically required by law to use competitive procurements. In order to participate in a procurement, a seller must either be directly invited by the buyer or satisfy a qualification process to be included in the bidding. For example, a seller with inadequate financial resources to ensure completion of a contract, or one that has performed poorly in the past, may be excluded from participation in a current procurement. In addition, a potential bidder that does not expend resources to qualify and that is unknown to the buyer may be excluded. For any typical competitive procurement, it is common for there to exist potential suppliers that are either not invited to bid or that do not seek qualification as a bidder.

Almost all procurement rules allow for the buyer, after receipt of all bids, to make no award and void the procurement. During the course of a procurement, a buyer may observe actions by the bidders, including their actual bids, that cause the buyer to believe that they are not obtaining the best value. In that case, a buyer may undertake some incremental action to invigorate the policing action of the competitive process and reconduct the procurement with this new competitive pressure in place. One such action is to invite and seek
qualification of sellers that did not participate in the initial round of bidding. If one or more new sellers can be identified, then the procurement may be reopened and new bids solicited.

Overall, a common sequence for procurements in private industry and the public sector is as follows.

1. **Initial bidding.** Invite qualified sellers to participate and obtain initial bids.
2. **Evaluation.** If the initial bids are “reasonable,” then make an award. If the bids provide the buyer with less surplus than expected, then consider voiding the initial procurement.
3. **Possible additional bidding.** If the initial procurement was voided, consider seeking additional competitive pressure, conducting a new procurement, and making an award based on the new bidding.

These common procurement practices guide our modeling framework.

In what follows, we provide a review of public procurements conducted by U.S. cities and towns, which generated the observations above. As background, in these procurements the bid specifications typically indicate that the city has the right to award the contract to the lowest responsive bidder, or to reject any and all bids.

In Table C.3, we summarize twenty recent examples of procurements in which all initial bids were rejected by the relevant government decision maker because the lowest responsive bid was unacceptably high for the buyer.\(^{44}\)

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\(^{44}\)The right to reject all bids can be exercised by government purchasing authorities for other reasons as well, e.g., bids are found to be non-responsive, bid documents are defective and/or incomplete, or there is evidence of inadequate competition.
Table C.3: Bid rejections and reprocurement

<table>
<thead>
<tr>
<th>City</th>
<th>Project</th>
<th>Industry</th>
<th>Number of Bidders</th>
<th>Date</th>
<th>Reason for Rejection</th>
</tr>
</thead>
<tbody>
<tr>
<td>Belmont</td>
<td>Overhaul and upgrade Sewer and Pump Station pumps, holding tanks, and consultants</td>
<td>Construction / Renovation</td>
<td>4</td>
<td>01.09.07</td>
<td>Not sufficient funding in project budget to award to low bidder</td>
</tr>
<tr>
<td>Belmont-2</td>
<td>Sanitary Sewer Rehabilitation Ralston Avenue Pipe Bursting and Pipelining</td>
<td>Construction / Renovation</td>
<td>2</td>
<td>09.14.04</td>
<td>Two received bids exceed the anticipates costs. The City will redesign and re-advertise the project</td>
</tr>
<tr>
<td>Clinton</td>
<td>Install water and sewer infrastructure for Sampson Square Apartments</td>
<td>Construction</td>
<td>3</td>
<td>02.16.10</td>
<td>Lowest bid greater than grant funding</td>
</tr>
<tr>
<td>Des Moines</td>
<td>Golf Course Repairs – damaged from erosion and slope failure</td>
<td>Construction</td>
<td>2</td>
<td>10.11.10</td>
<td>Lowest bid was 53% over project estimate and exceeded project budget</td>
</tr>
<tr>
<td>Folsom</td>
<td>Revitalization Project</td>
<td>Construction</td>
<td>2</td>
<td>07.20.09</td>
<td>Low bid exceeded engineer's estimate</td>
</tr>
<tr>
<td>Fresno</td>
<td>Delivery of Ortho Poly Phosphate Blend to the Surface Water Treatment Facility</td>
<td>Ortho Poly Phosphate Blend Delivery</td>
<td>1</td>
<td>05.01.07</td>
<td>Want to obtain greater bidder participation and lower pricing</td>
</tr>
<tr>
<td>Fresno-2</td>
<td>Landscaping around City Hall and Santa Fe Depot</td>
<td>Landscaping</td>
<td>4</td>
<td>10.02.07</td>
<td>There is a reasonable expectation that additional bids will be received through a future rebid, thereby, reducing the cost of this item</td>
</tr>
<tr>
<td>Lacey</td>
<td>Construct a treatment facility and booster station at reservoir site</td>
<td>Construction</td>
<td>5</td>
<td>05.24.07</td>
<td>Low bidder withdrew because of data errors and next apparent low bidder's value higher than engineer's estimate</td>
</tr>
<tr>
<td>Missoula</td>
<td>Stripping and stockpiling topsoil, and large rocks, rough grading, earth moving, landscape contouring and removal of excess granular materials</td>
<td>Construction</td>
<td>2</td>
<td>6.3.09</td>
<td>Both bids were above the anticipated budget for this project</td>
</tr>
<tr>
<td>Piedmont</td>
<td>Build children's play area</td>
<td>Construction</td>
<td>3</td>
<td>07.19.04</td>
<td>Large discrepancy between architect's estimate for the base bid work versus the low bid</td>
</tr>
</tbody>
</table>

45 We refer to the procurements by the name of the city. The full citations are provided at the end of this appendix.
In the cases we reviewed, it is common for the buyer (the city) to have comprehensive cost estimates of the project before soliciting bids. However, usually no formal reserve price is announced prior to bidding. It can happen that all received bids are beyond initial cost estimates or the cost limits established by the purchasing authorities. When the lowest received bid substantially exceeds the cost estimates or limits, the city councils may void the initial bids and announce reprocurement.

For example, in September 2006, the City Council of Belmont procured a contract for pump station rehabilitation. The contract was to be awarded to the lowest responsible bidder for an amount up to the engineer’s estimate of $520,000. Four general contractors submitted bids as follows: $695,000, $724,000, $787,000 and $859,000. After evaluation, the city council rejected all bids and re-advertised the project in Spring 2007.46

Bids may be rejected with the expectation of lower future bids. For example, Fresno’s reason for rejecting the bid it received in March 2007 was that: “There is a reasonable expectation that additional bids will be received through a future rebid, thereby, reducing

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46Belmont, pp.1–2.
the cost of this item.” 47 Lacey identified the possibility of seeking more competitive bids as a key reason for rebidding its contract. 48

In many of the examples listed in Table C.3, all bids were rejected because they were above what buyer believed to be a reasonable level. For example, Piedmont received three bids for its project, but there was a large discrepancy between the architect’s cost estimate for the project and the lowest bid. According to the staff report, “the difference between the base bid architect’s estimate and base bids actually received is obviously disappointing and troubling.” 49 The city council rejected all bids, re-worked the project specifications, and re-conducted the procurement. Folsom rejected all bids because “the lowest responsive bid was received from McGuire and Hester for $3,737,259.80 and was $1.55 million over the engineers estimate.” 50 San Rafael rejected all bids because “the lowest bid of $161,232.50 is $36,232.50 more than the Engineer’s Estimate.” 51 Villa Park rejected all bids due to the high cost of the lowest bid, which was above the engineer’s estimate. 52 Woodinville rejected all bids because “the low bid amount for this project exceeded the engineer’s estimate by approximately 30%.” 53

In other examples, the stated reason for rejection includes the low bid being above the approved budget for the project. 54

To summarize, a review of procurement examples reveals the following phenomena: 1. When the buyer is uncertain about the cost environment, it can infer information from the observed bids. 2. If the initial bids are viewed as reasonable, then the buyer makes an award to the lowest bidder. 3. If the initial bids are viewed as too high, the buyer may void the initial procurement and seek additional bidders to participate in a new procurement. 4. Budget-constrained buyers may reject bids even if there is no expectation of obtaining more favorable bids through reprocurement.

References for Online Appendix C.2


47 Fresno, p.4.
48 Lacey, paragraph 5.
49 Piedmont, p.1.
50 Folsom, p.3.
51 San Rafael, p.1.
52 Villa Park, p.1.
53 Woodinville, p.1.
54 See, e.g., Clinton, Des Moines, Missoula, Pinole, Plant City, Shasta Lake, Tracy, and Woodinville-2.


References


